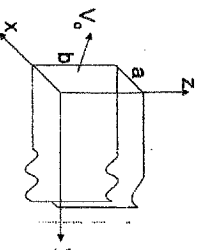


本考科禁用掌上型計算機

(請於此線以下開始出題)

- 5 (20%) 1. Suppose the electric field in some region is found to be $E = kr^3 \hat{r}$, in spherical coordinates (k is some constant).
- (a) Find the charge density ρ . (10%)
- (b) Find the total charge contained in a sphere of radius R , centered at the origin. (10%)

- 10 (20%) 2. An infinity long rectangular metal pipe (sides a and b) is ground, but one end, at $y=0$, is maintained at a specified potential $V(x, z) = V_0$ and the other four planes are $V=0$
- (a) Write down the Laplace equation of rectangular coordinates. (4%)
- (b) By using separation of variables, write down the solution of $X(x)$, $Y(y)$, and $Z(z)$. (6%)
- (c) Write down the total potential and find out the coefficient C_n . (10%)



- 15 (15%) 3. Show that vector potential $\vec{A} = \frac{1}{2} \vec{B} \times \vec{r}$ is a suitable solution for a uniform magnetic field of $\vec{B} = B_0 \hat{z}$. (15%)
- 20 (15%) 4. A sphere of linear magnetic material is placed in an otherwise uniform magnetic field B_0 . Find the new field inside the sphere. (15%)

- 25 (30%) 5. A uniform current density $\vec{j} = J_0 \hat{z}$ fills a slab standing the yz plane, from $x=-a$ to $x=+a$. A magnetic dipole $\vec{m} = m_0 \hat{x}$ is situated at the origin.
- (a) Find the force on the dipole. (5%)
- (b) Do the same for a dipole pointing in the y direction: $\vec{m} = m_0 \hat{y}$. (5%)
- (c) In the electrostatic case the expression $F = \nabla(p \cdot \vec{E})$ and $F = (p \cdot \nabla) \vec{E}$ are equivalent, but this is not the case for the magnetic analogs (explain why). (10%) As an example calculate $(\vec{m} \cdot \nabla) \vec{B}$ for the configuration in (a) and (b). (10%)